

Ex - 7.2

Q1. Find the co-ordinates of the point which divides the line joining of $(-1, 7)$ and $(4, -3)$ in the ratio $2 : 3$.

Sol. Let the required point be $P(x, y)$.

Here the end points are $(-1, 7)$ and $(4, -3)$

$$\therefore \text{Ratio} = 2 : 3 = m_1 : m_2$$

$$\therefore x = \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2} = \frac{(2 \times 4) + 3(-1)}{2 + 3}$$

$$= \frac{8 - 3}{5} = \frac{5}{5} = 1$$

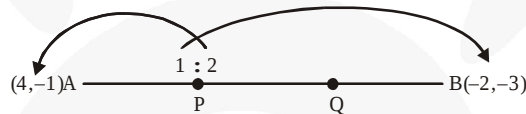
$$\text{And } y = \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2}$$

$$= \frac{2 \times (-3) + 3 \times 7}{2 + 3} = \frac{-6 + 21}{5} = \frac{15}{5} = 3$$

Thus, the required point is $(1, 3)$.

Q2. Find the coordinates of the points of trisection of the line segment joining $(4, -1)$ and $(-2, -3)$.

Sol.



Points P and Q trisect the line segment joining the points $A(4, -1)$ and $B(-2, -3)$, i.e., $AP = PQ = QB$.

Here, P divides AB in the ratio $1 : 2$ and Q divides AB in the ratio $2 : 1$.

$$\text{x-coordinate of P} = \frac{1 \times (-2) + 2 \times (4)}{1 + 2} = \frac{6}{3} = 2 ;$$

$$\text{y-coordinate of P} = \frac{1 \times (-3) + 2 \times (-1)}{1 + 2} = \frac{-5}{3}$$

Thus, the coordinates of P are $\left(2, -\frac{5}{3}\right)$.

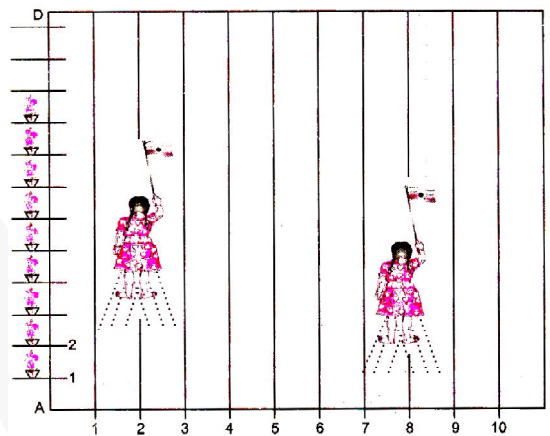
$$\text{Now, x coordinate of Q} = \frac{2 \times (-2) + 1 \times (4)}{2 + 1} = 0 ;$$

$$\text{y-coordinate of Q} = \frac{2 \times (-3) + 1 \times (-1)}{2 + 1} = -\frac{7}{3}$$

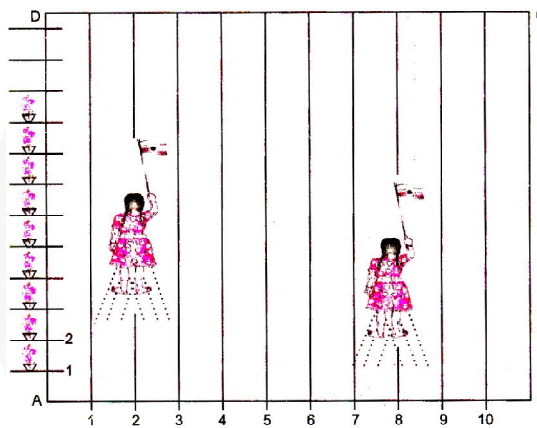
Thus, the coordinates of Q are $\left(0, -\frac{7}{3}\right)$.

Hence, the points of trisection are $P\left(2, -\frac{5}{3}\right)$ and $Q\left(0, -\frac{7}{3}\right)$.

- Q3.** To conduct Sports Day activities, in your rectangular shaped school ground ABCD, lines have been drawn with chalk powder at a distance of 1 m each. 100 flower pots have been placed at a distance of 1 m from each other along AD, as shown in fig. Niharika runs $\frac{1}{4}$ th the distance AD on the 2nd line and posts a green flag. Preet runs $\frac{1}{5}$ th the distance AD on the eighth line and posts a red flag. What is the distance between both the flags? If Rashmi has to post a blue flag exactly halfway between the line segment joining the two flags, where should she post her flag?



Sol. Let us consider 'A' as origin, then



AB is the x-axis.

AD is the y-axis.

Now, the position of green flag-post is

$$\left(2, \frac{100}{4}\right) \text{ or } (2, 25)$$

And, the position of red flag-post is

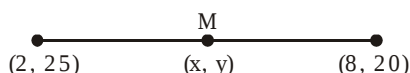
$$\left(8, \frac{100}{5}\right) \text{ or } (8, 20)$$

$\Rightarrow$ Distance between both the flags

$$= \sqrt{(8-2)^2 + (20-25)^2}$$

$$= \sqrt{6^2 + (-5)^2} = \sqrt{36 + 25} = \sqrt{61}$$

Let the mid-point of the line segment joining the two flags be M(x, y).



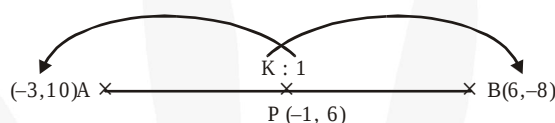
$$\therefore x = \frac{2+8}{2} \text{ and } y = \frac{25+20}{2}$$

or $x = 5$ and $y = 22.5$

Thus, the blue flag is on the 5th line at a distance 22.5 m above AB.

Q4. Find the ratio in which the line segment joining the points $(-3, 10)$ and $(6, -8)$ is divided by $(-1, 6)$.

Sol. Let the required ratio be $K : 1$



Comparing x-coordinate

$$\begin{aligned} \frac{k \times (6) + 1 \times (-3)}{k+1} &= -1 \\ \Rightarrow 6k - 3 &= -k - 1 \\ \Rightarrow 7k &= 2 \\ \Rightarrow k &= \frac{2}{7} \end{aligned}$$

Comparing y-coordinate

$$\begin{aligned} \frac{k \times (-8) + 1 \times (10)}{k+1} &= 6 \\ \Rightarrow -8k + 10 &= 6k + 6 \\ \Rightarrow -8K - 6K &= 6 - 10 \\ \Rightarrow -14K &= -4 \\ \Rightarrow k &= \frac{2}{7} \end{aligned}$$

Q5. Find the ratio in which the line segment joining

$A(1, -5)$ and $B(-4, 5)$ is divided by the x-axis. Also find the coordinates of the point of division.

Sol. The given points are : $A(1, -5)$ and $B(-4, 5)$. Let the required ratio = $k : 1$ and the required point be $P(x, y)$

Part-I : To find the ratio

Since, the point P lies on x-axis,

$\therefore$ Its y-coordinate is 0.

$$x = \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2} \text{ and } 0 = \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2}$$

$$\Rightarrow x = \frac{-4k + 1}{k + 1} \text{ and } 0 = \frac{5k - 5}{k + 1}$$

$$\Rightarrow x(k + 1) = -4k + 1$$

$$\text{and } 5k - 5 = 0 \Rightarrow k = 1$$

$$\Rightarrow x(k + 1) = -4k + 1$$

$$\Rightarrow x(1 + 1) = -4 + 1 \quad [\because k = 1]$$

$$\Rightarrow 2x = -3$$

$$\Rightarrow x = -\frac{3}{2}$$

$\therefore$ The required ratio $k : 1 = 1 : 1$

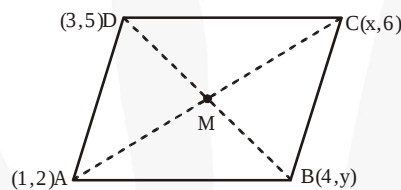
Coordinates of P are $(x, 0) = \left(-\frac{3}{2}, 0\right)$

Q6. If $(1, 2)$, $(4, y)$, $(x, 6)$ and $(3, 5)$ are the vertices of a parallelogram taken in order, find x and y .

Sol. Mid-point of the diagonal AC has x-coordinate

$$= \frac{x+1}{2} \text{ and y-coordinate} = \frac{6+2}{2} = 4$$

i.e., $\left(\frac{x+1}{2}, 4\right)$ is the mid-point of AC.



Similarly, mid-point of the diagonal BD is

$$\left(\frac{4+3}{2}, \frac{y+5}{2}\right), \text{ i.e., } \left(\frac{7}{2}, \frac{y+5}{2}\right)$$

We know that the two diagonals AC and BD bisect each other at M. Therefore,

$$\left(\frac{x+1}{2}, 4\right) \text{ and } \left(\frac{7}{2}, \frac{y+5}{2}\right) \text{ Coincide}$$

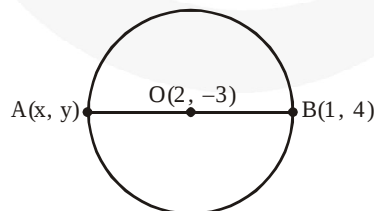
$$\Rightarrow \frac{x+1}{2} = \frac{7}{2} \text{ and } \frac{y+5}{2} = 4$$

$$\Rightarrow x = 6 \text{ and } y = 3$$

Q7. Find the coordinates of a point A, where AB is the diameter of a circle whose centre is $(2, -3)$ and B is $(1, 4)$.

Sol. Here, centre of the circle is $O(2, -3)$

Let the end points of the diameter be $A(x, y)$ and $B(1, 4)$



The centre of a circle bisects the diameter.

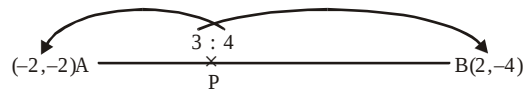
$$\therefore 2 = \frac{x+1}{2} \Rightarrow x+1 = 4 \text{ or } x = 3$$

$$\text{And } -3 = \frac{y+4}{2} \Rightarrow y+4 = -6 \text{ or } y = -10$$

Here, the coordinates of A are $(3, -10)$

Q8. If A and B are $(-2, -2)$ and $(2, -4)$, respectively, find the coordinates of P such that $AP = \frac{3}{7} AB$ and P lies on the line segment AB.

Sol.



$$AP = \frac{3}{7} AB,$$

$$BP = AB - AP = AB - \frac{3}{7} AB = \frac{4}{7} AB$$

$$\frac{AP}{BP} = \frac{\frac{3}{7} AB}{\frac{4}{7} AB} = \frac{3}{4}$$

Thus, P divides AB in the ratio 3 : 4.

$$\text{x-coordinate of P} = \frac{3 \times (2) + 4 \times (-2)}{3 + 4} = -\frac{2}{7}$$

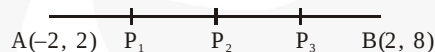
$$\text{y-coordinate of P} = \frac{3 \times (-4) + 4 \times (-2)}{3 + 4} = -\frac{20}{7}$$

Hence, the coordinates of P are $\left(-\frac{2}{7}, -\frac{20}{7}\right)$.

Q9. Find the coordinates of the points which divide the line segment joining A $(-2, 2)$ and B $(2, 8)$ into four equal parts.

Sol. Here, the given points are A $(-2, 2)$ and B $(2, 8)$

Let P_1 , P_2 and P_3 divide AB in four equal parts.



$$\therefore AP_1 = P_1P_2 = P_2P_3 = P_3B$$

Obviously, P_2 is the mid-point of AB

$\therefore$ Coordinates of P_2 are

$$\left(\frac{-2+2}{2}, \frac{2+8}{2}\right) \text{ or } (0, 5)$$

Again, P_1 is the mid-point of AP_2 .

$\therefore$ Coordinates of P_1 are

$$\left(\frac{-2+0}{2}, \frac{2+5}{2}\right) \text{ or } \left(-1, \frac{7}{2}\right)$$

Also P_3 is the mid-point of P_2B .

$\therefore$ Coordinates of P_3 are

$$\left(\frac{0+2}{2}, \frac{5+8}{2}\right) \text{ or } \left(1, \frac{13}{2}\right)$$

Thus, the coordinates of P_1 , P_2 and P_3 are $\left(-1, \frac{7}{2}\right)$, $(0, 5)$ and $\left(1, \frac{13}{2}\right)$ respectively.

Q10. Find the area of a rhombus if its vertices are (3, 0), (4, 5), (−1, 4) and (−2, −1) taken in order.

Sol. Diagonals AC and BD bisect each other at right angle to each other at O.

$$AC = \sqrt{(-1-3)^2 + (4-0)^2}$$

$$= \sqrt{16+16} = \sqrt{32} = 4\sqrt{2}$$

$$BD = \sqrt{(4+2)^2 + (5+1)^2} = \sqrt{36+36} = 6\sqrt{2}$$

$$\text{Then } OA = \frac{1}{2} AC = \frac{1}{2} \times 4\sqrt{2} = 2\sqrt{2}$$

$$OB = \frac{1}{2} BD = \frac{1}{2} \times 6\sqrt{2} = 3\sqrt{2}$$

$$\text{Area of } \triangle AOB = \frac{1}{2} (OA) \times (OB) = \frac{1}{2} \times 2\sqrt{2} \times 3\sqrt{2} = 6 \text{ sq. units}$$

Hence, the area of the rhombus ABCD

$$= 4 \times \text{area of } \triangle AOB = 4 \times 6 = 24 \text{ sq. units.}$$